The joint role of geometry and illumination on material recognition

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Observing and recognizing materials is a fundamental part of our daily life. Under typical viewing conditions, we are capable of effortlessly identifying the objects that surround us and recognizing the materials they are made of. Nevertheless, understanding the underlying perceptual processes that take place to accurately discern the visual properties of an object is a long-standing problem. In this work, we perform a comprehensive and systematic analysis of how the interplay of geometry, illumination, and their spatial frequencies affect human performance on material recognition tasks. We carry out large-scale behavioral experiments where participants are asked to recognize different reference materials among a pool of candidate samples. In the different experiments, we carefully sample the information in the frequency domain of the stimuli. From our analysis, we find significant first-order interactions between the geometry and the illumination, of both the reference and the candidates. In addition, we observe that simple image statistics and higher-order image histograms do not correlate with human performance. Therefore, we perform a high-level comparison of highly nonlinear statistics by training a deep neural network on material recognition tasks. Our results show that such models can accurately classify materials, which suggests that they are capable of defining a meaningful representation of material appearance from labeled proximal image data. Last, we find preliminary evidence that these highly nonlinear models and humans may use similar high-level factors for material recognition tasks.

Introduction

Under typical viewing conditions, humans are capable of effortlessly recognizing materials and inferring many of their key physical properties, just by briefly looking at them. Although this is almost an effortless process, it is not a trivial task. The image that is input to our visual system results from a complex combination of the surface geometry, the reflectance of the material, the distribution of lights in the environment, and the observer’s point of view. To recognize the material of a surface while being invariant to other factors of the scene, our visual system carries out an underlying perceptual process that is not yet fully understood (Adelson, 2000; Dror et al., 2001a; Fleming et al., 2001).

So how does our brain recognize materials? We could think that, similar to solving an inverse optics problem, our brain is estimating the physical properties of each material (Pizlo, 2001). This would imply knowledge of many other physical quantities about the object and its surrounding scene, from which our brain could disentangle the reflectance of the surface. However, we rarely have access to such precise information, so variations based on Bayesian inference have been proposed (Kersten et al., 2004).

Other approaches are based on image statistics, and explain material recognition as a process where our brain extracts image features that are relevant to describe materials. Then, it would try to match them with previously acquired knowledge, to discern the material we are observing. Considering this approach our visual system would disregard the illumination, motion, or other factors in the scene and try to recognize materials by representing their typical appearance in terms of features instead of explicitly acquiring an accurate physical description of each factor. This type of image analysis can be carried out in the primary domain (Adelson, 2008; Fleming, 2014; Geisler, 2008; Motoyoshi et al., 2007; Nishida & Shinya, 1998), or in the frequency domain (Brady & Oliva, 2001).
Figure 1. Two spheres made of silver, under two different illuminations, leading to completely different pixel-level statistics.

Figure 2. Two objects of different geometries but made of the same material, under the same illumination. The object on the left seems to be made of a shinier material.

Material recognition

Recognizing materials and inferring their key features by sight is invaluable for many tasks. Our experience suggests that humans are able to correctly predict a wide variety of rough material categories like textiles, stones, or metals (Fleming & Bulthoff, 2005; Fleming, 2014; Ged et al., 2010; Li & Fritz, 2012); or items that we would call “stuff” (Adelson, 2001)—like sand or snow. Humans are also capable of identifying the materials in a photograph by briefly looking at them (Sharan et al., 2009, 2008) or of inferring their physical properties without the need to touch them (Fleming et al., 2013, 2015a; Jarabo et al., 2014; Maloney & Brainard, 2010; Nagai et al., 2015; Serrano et al., 2016). This ability is built from experience, by actually confirming visual impressions with other senses. This way, material perception becomes a cognitive process (Palmer, 1975) whose underlying intricacies are not fully understood yet (Anderson, 2011; Fleming et al., 2015b; Thompson et al., 2011).

Interplay of geometry and illumination

Material perception is a complex process that involves a large number of distinct dimensions (Mao et al., 2019; Obein et al., 2004; Sève, 1993) that, sometimes, are impossible to physically measure (Hunter et al., 1937). The illumination of a scene (Beck & Prazdny, 1981; Bousseau et al., 2011; Zhang et al., 2015) and the shape of a surface, are responsible for the final appearance of an object (Nishida & Shinya, 1998; Schlüter & Faul, 2019; Vangorp et al., 2007) and, therefore, for our perception of the materials it is made of (Olkkonen & Brainard, 2011). Humans are capable of estimating the reflectance properties of a surface (Dror et al., 2001b) even when there is no information about its illumination (Dror et al., 2001a; Fleming et al., 2001), yet we perform better under illuminations that match real-world statistics (Fleming et al., 2003). Indeed, geometry and illumination have a joint interaction in our perception of glossiness (Faul, 2019; Leloup et al., 2010; Marlow et al., 2012; Olkkonen & Brainard, 2011) and color (Bloj et al., 1999). In this work, we explore the interplay of shape, illumination, and their spatial frequencies in our performance at recognizing materials. To achieve that, we launched rigorous online behavioral experiments where we rely on realistic computer graphics to generate the stimuli and carefully vary their information in the frequency domain.
Image statistics and material perception

One of the goals in material perception research is to untangle the processes that happen on our visual system to comprehend their roles and know what information they carry. There is an ongoing discussion on whether our visual system is solving an inverse optics problem (Kawato et al., 1993; Pizlo, 2001) or if it matches the statistics of the input to our visual system (Adelson, 2000; Motoyoshi et al., 2007; Thompson et al., 2016) to understand the world that surrounds us. Later studies regarding our visual system and how we perceive materials dismiss the inverse optics approach and claim that it is unlikely that our brain estimates the parameters of the reflectance of a surface, when, for instance, we want to measure glossiness (Fleming, 2014; Geisler, 2008). Instead, they suggest that our visual system joins low and midlevel statistics to make judgments about surface properties (Adelson, 2008).

On this hypothesis, Motoyoshi et al. (2007) suggest that the human visual system could be using some sort of measure of histogram symmetry to distinguish glossy surfaces. Other works have explored image statistics in the frequency domain (Hawken & Parker, 1987; Schiller et al., 1976), for instance, to characterize material properties (Giesel & Zaidi, 2013), or to discriminate textures (Julesz, 1962; Schaffalitzky & Zisserman, 2001). However, it is argued that, if our visual system actually derives any aspects of material perception from simple statistics (Anderson & Kim, 2009; Kim & Anderson, 2010; Olkkonen & Brainard, 2010). Instead, recent work by Fleming and Storrs (2019) proposes that, to infer the properties of the scene, our visual system is doing an efficient and accurate encoding of the proximal stimulus (image input to our visual system). Thus, highly nonlinear models, such as deep neural networks, may better explain human perception. In line with such observations, Bell et al. (2015) show how deep neural networks can be trained in a supervised fashion to accurately recognize materials, and Wang et al. (2016) later extend it to also recognize materials in light fields. Closer to our work, Lagunas et al. (2019) devise a deep learning-based material similarity metric that correlates with human perception. They collected judgements on perceived material similarity as a whole, not explicitly taking into account the influence of geometry or illumination, and build their metric upon such judgements. In contrast, we focus on analyzing to which extent geometry and illumination do interfere with our perception of material appearance. We launch several behavioral experiments with carefully controlled stimuli, and ask participants to specify which materials are closer to a reference. In addition, taking inspiration from these recent works, we explore how highly nonlinear models, such as deep neural networks, perform in material classification tasks. We find that such models are capable of accurately recognizing materials, and further observe that deep neural networks may share similar high-level factors to humans when recognizing materials.

Methods

We carried out a set of online behavioral experiments where we analyze the influence of geometry, illumination, and their frequencies in human performance for material recognition tasks. Participants are presented with a reference material and their main task is to pick five materials from a pool of candidates that they think are closer to the reference. A screenshot of the experiment can be seen in Figure 3.

Stimuli

We obtain our stimuli from the dataset proposed by Lagunas et al. (2019). This dataset contains images created using photorealistic computer graphics, with 15 different geometries, 6 different real-world illuminations ranging from indoor scenarios to urban or natural landscapes, and 100 different materials measured from their real-world counterparts which were pooled from Mitsubishi Electric Research Laboratories (MERL) database (Matusik et al., 2003). We sample the following factors for our experiments:

Geometries. Among the geometries that the dataset contains, we choose the sphere and Havran-2 geometry (Havran et al., 2016). These are low and high spatial frequency geometries, respectively, suitable to test how the spatial frequencies of the geometry affect the final appearance of the material and our performance at recognizing it.

• Sphere: Representing a smooth, and low spatial frequency geometry, widely adopted in previous
behavioral experiments (Filip et al., 2008; Jarabo et al., 2014; Kerr & Pellacini, 2010; Sun et al., 2017).

- **Havran-2.** It is a geometry with high spatial frequencies, and with high spatial variations that has been obtained through optimization techniques.
- **Havran-2:** Surface has had significant success in recent perceptual studies and applications (Guarnera et al., 2018; Guo et al., 2018; Lagunas et al., 2019; Vávra & Filip, 2016).

The stimuli in each different experiment can be observed in Figure 4. The geometry in the reference and candidate samples changes depending on the experiment, the details are as follows:

- **Test HH:** Both the reference and the candidates depict *Havran* geometry.
- **Test HS:** The reference depicts *Havran* and the candidates depict the sphere.
- **Test SH:** The reference depicts the sphere while the candidates depict *Havran*.
- **Test SS:** Both the reference and the candidates depict the sphere geometry.

**Illuminations.** To prevent a pure matching task, we choose different illuminations between the reference and candidate materials for all behavioral experiments.

- The reference samples depict six different illuminations captured from the real world. All illuminations can be observed in Figure 5. To have an intuition of the content in the captured illumination, the insets show the RGB intensity for the horizontal purple line. We use all illuminations in the dataset since they contain a mix of spatial frequencies suitable to empirically test how the spatial frequencies of the illumination may affect human performance on material recognition tasks. The illuminations *Grace, Ennis,* and *Uffizi* have a broad spatial frequency spectrum, *Pisa* and *Doge* mainly contain medium and low-spatial frequency content, while *Glacier* mainly has low-spatial frequency content. To simplify the notation, we refer to them throughout the article as high-frequency, medium-frequency, and low-frequency illuminations, respectively.
- The candidate samples depict the *St. Peters* illumination (except in an additional experiment discussed in the Discussion where they depict *Doge* illumination). *St. Peters* is an illumination that has been used in the past for several perceptual studies (Fleming et al., 2003; Serrano et al., 2016), and it can be seen in Figure 5. The inset shows the RGB pixel intensity for the horizontal purple line.

To quantify the spatial frequencies of the illuminations, we have employed the high-frequency content (HFC) measure (Brossier et al., 2004). This measure characterizes the frequencies in a signal by summing linearly weighted values of the spectral magnitude, thus avoiding to arbitrarily choose a separation between high and low frequencies, or visually assessing the slope of the 1/f amplitude spectrum. A high HFC value means higher frequencies in the signal. Figure 6 shows the HFC for each illumination.

**Materials**

We use all the materials from the Lagunas et al. dataset Lagunas et al. (2019). The reference trials are
samples uniformly to cover all 100 material samples in the dataset. Examples of the stimuli used in each behavioral experiment are shown in Figure 4, where the image on the left shows the reference material and the right area shows a subset of the candidate materials.

**Participants**

The online behavioral experiments were designed to work across platforms on standard web browsers, and they were conducted through the Amazon Mechanical Turk (MTurk) platform. In total, 847 unique users took part in them (368 users belonging to the experiments explained in Results, and 479 belonging to the additional experiments explained in Discussion), 44.61% of them female. Among the participants, 62.47% claimed to be familiar with computer graphics, 25.57% had no previous experience and 9.96% declared themselves professionals. We also sampled data regarding the devices used during the experiments: 94.10% used a monitor, 4.30% used a tablet, and 1.60% used a mobile phone. In addition, the most common screen size was 1366 × 728 pixels (42.01% of participants), minimum screen size was 640 × 360 pixels (two people), and a maximum of 2560 × 1414 pixels (one person). Users were not aware of the purpose of the behavioral experiment.

**Procedure**

Subjects are shown a reference sample and a group of candidate material samples. Each experiment, HIT in MTurk terminology, consists of 23 unique reference material samples or trials, 36 of which are sentinels used to detect malicious or lazy users. Users are asked to “select five material samples which you believe are closer to the one shown in the reference image.” Additionally, we instruct them to make their selection in decreasing order of confidence. We let the users pick five candidate materials because just one answer would provide sparse results. We launched 25 HITs for each experiment and each HIT was answered by six different users. This resulted in a total of 27,000 nonsentinel trials, 12,000 belonging to the four experiments analyzed in the Results, and 15,000 of them belonging to the five additional experiments discussed in the Discussion (a total of nine different experiments with 25 HITs each, each HIT answered by six users and 20 nonsentinel trials per HIT). Users were not allowed to repeat the same HIT.

The set of materials in the candidate samples does not vary across HITs; however, the position of each sample is randomized for each trial. This has a two-fold purpose: it prevents the user from memorizing the position of the samples, and it prevents them from selecting only the candidate samples that appear at the top of their screen. The reference samples do not repeat materials during a HIT and the reference material is always present among the candidate samples. During the experiment, stimuli keep a constant display size of 300 × 300 pixels for the reference, and of 120 × 120 pixels for the candidate stimuli (except for some of the additional experiments explained in Discussion where both reference and candidate stimuli are displayed at either 300 × 300 pixels or 120 × 120 pixels). Figure 3 shows a screenshot with the graphical user interface during the behavioral experiments. On the left-hand side, we can observe the selection panel with the current trial and the selection of the current materials. The right-hand side displays the set of candidate materials whereof users can pick their selection. Users were not able to go back and redo an already answered trial, but they could edit their current selection of five materials until they were satisfied with their choice. Additionally, once the 23 trials of the HIT are answered, to have an intuition about the main features that humans use for material recognition, we asked the user: “Which visual cues did you consider to perform the test?”

To minimize worker unreliability, the user performs a brief training before the real test (Welinder et al., 2010). To avoid giving the user further information about the test, we use a different geometry (Havran-3 Havran et al., 2016) during the training phase. In this phase, the items of the interface are explained and the user is given guidance on how to perform the test using just a few images (Garces et al., 2014; Lagunas et al., 2018; Rubinstein et al., 2010).

**Sentinels**

Each sentinel shows a randomly selected image from the pool of candidates as the reference sample. We consider user answers to the sentinel as valid if they pick...
the right material within their five selections, regardless of the order. We rejected users who did not correctly answer at least one of the three sentinel questions. To ensure that users’ answers were well thought and that they were paying attention to the experiment, we also rejected users that took less than 5 seconds per trial (on average). In the end, we adopt a conservative approach and rejected 19.8% of the participants, gathering 21,660 answers (9,560 belonging to the behavioral experiments explained in the Results and 12,100 belonging to the additional experiments explained in the Discussion).

Results

We investigate which factors have a significant influence on user performance and on the time they took to complete each trial in the four experiments: Test HH, Test HS, Test SH, and Test SS. The factors we include are: the reference geometry $G_{\text{ref}}$, the candidate geometry $G_{\text{cand}}$, and the illumination of the reference sample $I_{\text{ref}}$, as well as their first-order interactions (recall that the illumination of the candidate samples remains constant in these behavioral experiments). We also include the Order of appearance of each trial. We use a general linear mixed model with a binomial distribution for the performance since it is well-suited for binary dependent variables like ours, and a negative binomial distribution for the time, which provides more accurate models than the Poisson distribution by allowing the mean and variance to be different. Because we cannot assume that our observations are independent, we model the potential effect of each particular subject viewing the stimuli as a random effect. Because we have categorical variables among our predictors, we re-code them to dummy variables for the regression. In all our tests, we fix a significance value ($P$-value) of 0.05. Finally, for factors that present a significant influence, we further perform pairwise comparisons for all their levels (least significant difference pairwise multiple comparison test).

Analysis of user performance and time

In our online behavioral experiments, we rely on the top five accuracy to measure user performance. This metric considers an answer as correct if the reference is among the five candidate materials that the user picked in the trial. Because participants picked five materials ranked in descending order of confidence, the top one accuracy could also be considered for our analysis. However, the task they have to solve is not easy and users have an overall top one accuracy of 9.21% which yields sparse results. A random selection would yield a top one accuracy of 1% and a top five accuracy of 5%.

Influence of the geometry

There is a clear effect in user performance when the geometry changes, regardless if that change happens in the candidate ($G_{\text{cand}}$, $P = 0.005$) or the reference geometry ($G_{\text{ref}}$, $P < 0.001$). This finding is expected, because the geometry plays a key role in how a surface reflects the incoming light and, therefore, will have an impact on the final appearance of the material. Figure 7 shows user performance in terms of top five accuracy with a 95% confidence interval when the reference and candidate geometry change jointly (left) or individually (center and right). Users seem to perform better when they have to recognize the material in a high-frequency geometry compared with a low-frequency one. Those results also suggest that changes in the frequencies of the reference geometry may have a bigger impact on user performance than changes in the frequencies of the candidate geometry (i.e., users perform better with a high-frequency reference geometry and low-frequency candidate geometry, compared to a low-frequency reference geometry and a high-frequency candidate geometry).

Influence of the reference illumination

We observe that the illumination of the reference image has a significant effect on user performance ($I_{\text{ref}}$, $P < 0.001$). This finding is expected because all the materials in a scene are reflecting the light that reaches them; therefore, the changes in illumination can significantly influence the final appearance of a material, and how we perceive it (Bousseau et al., 2011). Figure 8, left, shows the top five accuracy for each reference illumination and groups of illuminations with statistically indistinguishable performance. We can
observe how users seem to have better performance when the surface they are evaluating has been lit with a high-frequency illumination (Ennis, Grace, and Uffizi), whereas users seem to perform worse in scenes with a low-frequency illumination (Glacier); users show an intermediate performance with a medium-frequency illumination (Doge and Pisa). Moreover, we performed a least significant difference pairwise multiple comparison test to obtain groups of illuminations with statistically indistinguishable performance. These groups can be observed in Figure 8, under the x-axis. If we focus on Iref we can see how high- (green), medium- (blue), and low-frequency (red) illuminations yield groups of similar performance. There is an additional group of statistically indistinguishable performance represented in pink.

**Influence of trial order**

The order of appearance of the trials during the experiment does not have a significant influence in users performance (Order, P = 0.391).

**First order interactions**

We find that the interaction between the candidate geometry and the reference illumination has a significant effect on user performance (Gcand * Iref, P < 0.001). Users seem to perform better with a high-frequency geometry (compared with a low-frequency one) when the reference stimuli features a high-frequency illumination (Iref = Uffizi, P = 0.019; Iref = [Grace, Ennis], P < 0.001). On the other hand, there seems to be no significant changes in performance between a high- and low-frequency candidate geometry when the reference stimuli has a medium- or low-frequency illumination (Iref = Doge, P = 0.453; Iref = Pisa, P = 0.381; Iref = Glacier, P = 0.770). We argue that user performance is driven by the reference sample. When the reference material is lit with a low-frequency illumination, users seem to not be able to properly recognize it. Therefore, changes in the candidate geometry are not relevant to user performance. These results can be seen in Figure 8, center. Furthermore, under the x-axis, we can observe the groups with statistically indistinguishable performance where high-, medium-, and low-frequency illuminations yield groups of similar performance.

We also found out that the interaction between the reference geometry and the reference illumination has a significant impact in user performance (Gref * Iref, P = 0.012). Users seem to show better performance for all illuminations with a high-frequency reference geometry (Gref = Havran, Iref = Uffizi, P = 0.002; Iref = [Ennis, Pisa, Doge, Glacier], P < 0.001), except for Grace illumination (P = 0.176), where the differences in humans performance are statistically indistinguishable. These results, together with the groups of statistically indistinguishable performance, can be seen in Figure 8, right.
Figure 9. Visualizations of user answers to each of the four online behavioral experiments (namely, TEST HH, TEST HS, TEST SH, and TEST SS) using the t-STE algorithm (Van Der Maaten & Weinberger, 2012). The inset shows the color of each material based on the color classification proposed by Lagunas et al. (2019). We can see how, for all experiments, materials with similar color properties are grouped together. Furthermore, if we explore the color clusters individually, we can see how there is a second-level arrangement by reflectance properties. These observations suggest that users may be performing a two-step process while recognizing materials where first, they sort them out by color, and second, by reflectance properties.

In general, we cannot conclude that there are significant changes in performance due to the interaction between the candidate and reference geometry ($G_{ref} \times G_{cand}$, $P = 0.407$). Nevertheless, with a low-frequency reference geometry ($G_{ref} = sphere$), users seem to perform significantly better with a high-frequency candidate geometry ($G_{cand} = Havran$, $P = 0.009$).

Analysis of the time spent on each trial

To account for time, we measure the number of milliseconds that passed since the trial loaded in their screen and until they picked all five materials and pressed the “Continue” button.

Influence of trial order

We find that the order of the trials has a significant influence on the average time users spend to answer them ($P < 0.001$). Users spend more time in the first questions and that after few trials the average time they spend becomes stable at around 20 seconds per trial (recall that the order does not influence performance). This phenomenon is expected as users have to familiarize with the experiment during the first iterations. As the test advances, they learn how to interact with it and the time they spend becomes stable. Additional figures and results on the factors that influence the spent time can be found in Appendix A.

High-level factors driving material recognition

In addition to the analysis, we also try to gain intuition on which high-level factors drive material recognition, investigate how simple image statistics and image histograms correlate with human answers, and analyze highly nonlinear statistics in material classification tasks by training a deep neural network.

Visualizing user answers

To gain intuition on which high-level factors humans might use while recognizing materials, we use a stochastic triplet embedding method called the (t-Student stochastic triplet embedding (t-STE)) (Van Der Maaten & Weinberger, 2012) directly on user answers. This method maps user answers from their original non-numerical domain into a two-dimensional space that can be easily visualized (find additional details in the Appendix B). Figure 9 shows the two-dimensional embeddings after applying the t-STE algorithm to the answers of each online behavioral experiment. Each point in the embedding represents 1 of the 100 materials from the Lagunas et al. dataset. The insets show the color of each material based on the color classification proposed by Lagunas et al. We can observe how materials are clustered by color and, if we focus in a single color, they seem to be clustered by reflectance properties (e.g., in Test HH, red color cluster, we can observe how on the left there are specular materials while on the right there are diffuse materials). This finding suggests that users have followed a two-step strategy to recognize the materials, and that the high-level factors driving material recognition might be color first, and the reflectance properties second. At the end of the HIT, users were asked to write the main visual features they used to recognize materials. Out of 368 unique users from the experiments analyzed in the Results, 273 answered that they have used the colors, and 221 answered that they relied on the reflections. Among them, 157 answered both color and reflections.
as some of the visual cues they have used to perform the task. This observation, together with the t-STE visualization, strengthens the hypothesis of a two-step strategy.

**Image statistics**

Previous studies focused on simple image statistics as an attempt to further understand our visual system (Adelson, 2008; Motoyoshi et al., 2007). Nevertheless, it is argued whether our visual system actually derives any aspects of material perception using such simple statistics (Anderson & Kim, 2009; Kim & Anderson, 2010; Olkkonen & Brainard, 2010). We tested the correlation between the first four statistical moments of the luminance (considered as the ratio: \( L = 0.3086 \times R + 0.6094 \times G + 0.0820 \times B \)), the pixel intensity for each color channel independently, and the joint RGB pixel intensity, directly against users top five accuracy. To measure correlation we employ a Pearson \( P \) and Spearman \( S \) correlation test. We found out that there is little to no correlation, except for the standard deviation of the joint RGB pixel intensity where \( P^2 = 0.43 (P < 0.001) \) and \( S^2 = 0.50 (P < 0.001) \). Additional information can be found in Appendix C.

**Image histograms**

We also compute the histograms of the RGB pixel intensity, of the luminance, of a Gaussian pyramid (Lee & Lee, 2016), of a Laplacian pyramid (Burt & Adelson, 1983), and of log-Gabor filters designed to simulate the receptive field of the simple cells of the Primary Visual Cortex (V1) (Fischer et al., 2007). To see how such histograms would perform at classifying materials, we train a support vector machine (SVM) that takes the image histogram as the input and classifies the material in that image. We use a radial basis function kernel (or Gaussian kernel) in the SVM. We use all image histograms that do not feature Havran geometry as the training set and leave the ones with Havran as test set. In the end, the best performing SVM uses the RGB image histogram as the input and achieves a 24.17% top five accuracy in the test set.

In addition, we compare the predictions of each SVM directly against human answers. For each reference stimuli we compare the five selections of the user against the five most likely SVM material predictions for that stimuli. The best SVM uses the histograms of V1-like subband filters and agrees with humans 6.36% of the time. Moreover, we compare histogram similarities against human answers using a \( X^2 \) histogram distance (Pele & Werman, 2010). For a reference image stimuli we measure its similarity against all possible candidate image stimuli and compare the closest five against participants answers. The Gaussian pyramid histogram obtained the best result, agreeing with humans 6.29% of the time. These results show how simple statistics, and higher-order image histograms seem not to be capable of fully capturing human behavior. We have added additional results on the SVMs and human agreement in Appendix C.

**Image frequencies**

To understand if humans’ performance could be explained by taking into account the spatial frequency of the reference stimuli, at their viewed size, we have added the HFC measure, and the first four statistical moments of the reference stimuli magnitude spectrum to the factors analyzed in the Results. We found that the Skewness \( (P < 0.001) \) and Kurtosis \( (P < 0.001) \) of the magnitude spectrum seem to have a significant influence on humans performance; however, they present a very small effect size.

**Highly nonlinear models**

Recent studies suggest that, to understand what surrounds us, our visual system is doing an efficient nonlinear encoding of the proximal stimulus (the image input to our visual system) and that highly nonlinear models might be able to better capture human perception (Delanoy et al., 2020; Fleming & Storrs, 2019). Inspired by this hypothesis, we have trained a deep neural network called ResNet (He et al., 2016) using a loss function suitable to classify the materials in the Lagunas et al. dataset. The images feature the same illuminations as the reference stimuli. We left out the images rendered with Havran geometries for validation and testing purposes, and use the rest during training. To know which material the network classifies we add a softmax layer at the end of the network. The softmax layer outputs the probability of the input image to belong to each material in the dataset. In comparison, the model used by Lagunas et al. does not have the last fully connected and softmax layer, and it is trained using a triplet loss function aiming for similarity instead of classification. At the end of the training, the model achieves a top-5 accuracy of 89.63% on the test set, suggesting that such models are actually capable of extracting meaningful features from labeled proximal image data (additional details on the training can be found in Appendix D). To gain intuition on how the network has learned, we have used the Uniform Manifold Approximation and Projection algorithm (McInnes & Healy, 2018). This algorithm aims to decrease the dimensionality of a set of feature vectors while maintaining the global and local structure of their original manifold. Figure 10 shows a two-dimensional visualization of the test set obtained using the 128 features of the fully connected layer before softmax. We can observe how materials seem to be grouped first by color and then by its reflectance properties suggesting...
that the model may have used similar high-level factors to humans when classifying materials.

We additionally assess the degree of similarity between the high-level visualization of each online behavioral experiment and the high-level visualization of the deep neural network. We calculate the similarity in a pairwise fashion where we choose a material sample and retrieve its five nearest neighbors in two different low-dimensional representations. Then, we compute the percentage of materials that are the same in both groups of nearest neighbors. We repeat this process for all the materials and calculate the similarity as the average. The low-dimensional representations are obtained with stochastic methods, where the same input can have different results if we vary the parameters. To evaluate the degree of self-similarity, we run the t-STE algorithm (Van Der Maaten & Weinberger, 2012) on each behavioral experiment using five different sets of fully randomly sampled parameters. We obtain a self-similarity value of 0.66, on average across experiments. In contrast, a set of random low-dimensional representations has a similarity of 0.06, on average. Figure 11 shows the average pairwise similarity normalized by the value of self-similarity and random similarity for all experiments and the deep neural network visualization. If we compare the behavioral experiments, we can observe a decreasing degree of similarity because their stimuli feature fewer frequencies in the spectrum, where Test SS yields the lowest similarity in each of the pairwise comparisons. We argue that Test SS has the lowest similarity because it is the experiment where users have the worst performance, thus yielding a blurry high-level visualization. In contrast, the network is very accurate at classifying materials and yields a high-level visualization with well-defined material clusters. Moreover, if we focus on the deep neural network visualization, we can observe how its similarity values are, in general, on par with those obtained by users in Test HH, Test HS, and Test SH. This result further supports the hypothesis that both humans and deep neural networks may rely on similar high-level visual features for material recognition tasks. However, this is just a preliminary result that may highlight a future avenue of research, and a thorough analysis of the perceptual relationship between deep learning architectures and humans is out of the scope of this article.

**Discussion**

From our online behavioral experiments, we have observed that humans seem to perform better at recognizing materials in stimuli with high-frequency illumination and geometry. Moreover, our performance when recognizing materials is poor on low-frequency illuminations, and it remains statistically indistinguishable irrespective of the spatial frequency content in the candidate geometry.

Figure 11. Normalized pairwise similarity for each online behavioral experiment and the deep neural network trained for material classification. We can observe how the pairwise similarity decreases as the stimuli in the experiments cover fewer frequencies in the spectrum, where Test SS has the lowest similarity. Additionally, we can see how the similarities between the neural network and each behavioral experiment are on par with those obtained by humans between Test HH, Test HS, and Test SH. DNN, deep neural network.
Figure 12. Top five accuracy obtained by participants in the original experiment (left), when the stimuli are displayed at 300 × 300 pixels (middle), and at 120 × 120 pixels (right). We can observe how the asymmetric effect of participants performing better when Havran is the reference geometry (TestHS) compared with when it is the candidate (TestSH) remains present when the participants observe the reference and candidate stimuli at identical sizes (middle and right). The * denotes significant differences. The error bars correspond with a 95% confidence interval.

Asymmetric effect of the reference and candidate geometry

It is also interesting to observe that humans seem to have better performance with a high-frequency reference geometry, compared to a high-frequency candidate geometry ($P = 0.001$, Figure 12, left). The number of candidates with respect to the reference could be used as an explanation for this observation, since users may devote more time to inspecting the single reference than the higher number of candidates. At the same time, a lower performance with a high-frequency reference geometry may speak against an inverse optics approach because having multiple candidate materials with the same geometry and illumination could provide a strong cue to inferring the material.

One potential factor that may explain this difference in performance is the different display sizes of the reference (300 × 300 pixels) and the candidate (120 × 120 pixels) stimuli. To test this hypothesis, we have launched two additional experiments where we collect answers on Test HS and Test SH displaying the candidate and the reference stimuli at size 300 × 300, and other two additional experiments where they are displayed at 120 × 120 pixels. We sample the stimuli to cover all the possible combinations of illuminations and materials and keep other technical details as explained in the Methods. We perform an analysis of the gathered data similar to the one explained in the Results, but using the different experiment type as a factor. From our results, we observe that such asymmetric effect remains present when the stimuli are displayed at 300 × 300 pixels ($P < 0.001$) and when they are displayed at 120 × 120 pixels ($P < 0.001$). Those results can be seen in Figure 12, middle and right. It is also interesting to observe how users have slightly worse performance when the stimuli are displayed at 300 × 300 pixels. At such a display size, only three candidate stimuli per row could be displayed taking into account the most used display size. Thus, it seems reasonable to think that the need for additional scrolling could be hampering participants performance.

Influence of the candidate illumination

We have seen that humans seem to be better at recognizing materials under high-frequency reference illuminations. However, in Figure 5 and 6 we can see that the St. Peters candidate illumination features a similar frequency content to the reference illuminations where users have better performance. To assess if St. Peters illumination contains a set of frequencies that aids recognizing materials under reference illuminations with a similar set of frequencies, we have launched an additional behavioral experiment. In this experiment we use Doge, a medium-frequency illumination, as the candidate illumination. We sample the stimuli to cover all materials and reference illuminations in Test HH. Other technical details are kept as explained in the Methods. From the data collected (Figure 13), we can
observe how, using *Doge* as the candidate illumination, humans perform best when the candidate illumination matches the original illumination (with *St. Peters* as the candidate illumination). Participants perform better with high-frequency reference illuminations (*Uffizi, Grace, Ennis*), they perform worse with medium-frequency ones (*Pisa*), and have their worst performance with low-frequency reference illuminations (*Glacier*). In addition, participants seem to have slightly better performance with a high-frequency candidate illumination (*St. Peters*) compared with a medium-frequency one (*Doge*).

**Interplay between material, geometry, and illumination**

We have looked into how geometry, illumination, and their frequencies affect our performance in material recognition tasks. Our stimuli were rendered images in which we varied the frequency of the illumination, and of the underlying geometry of the object present. To better understand how our factors (illumination and geometry) affect the generated stimuli, and thus the proximal stimulus, we offer here a brief description of the rendering equation, providing an explanation of the probable effect of how the frequencies of the geometry and illumination in the 3D scene affect the final, rendered image that is used as a stimulus in our experiments. From the point of view of the rendering equation, the radiance $L_i$ at point $x$ in direction $\omega_i$, assuming a distant illumination and nonemissive surfaces can be approximated as

$$L_o(x, \omega_i) \approx \int_{\Omega} L_i(\omega_i) F(\omega_i, \omega_o) T(x, \omega_i, \omega_o) \, d\omega_i,$$  \hspace{1cm} (1)

where $L_i$ accounts for the incoming light, the variable $F$ accounts for the reflectance of the surface, and $T$ depends on the point of the surface we are evaluating, therefore, on the geometry.

The simulation of the radiance $L_o$ can be seen as a convolution (spherical rotation) (*Ramamoorthi & Hanrahan, 2001*) between each signal: incoming radiance $L_i$, material $F$, and geometry $T$. Moreover, if we analyze $L_o$ in the frequency domain (where $\mathcal{F}$ is the Fourier transform), and apply the convolution theorem ($f \ast g = \mathcal{F}(f) \cdot \mathcal{F}(g)$) the value of $\mathcal{F}(L_o)$ becomes

$$\mathcal{F}(L_o) \approx \mathcal{F}(L_i) \mathcal{F}(F) \mathcal{F}(T).$$ \hspace{1cm} (2)

Equation (2) shows how the frequency of the radiance $L_o$ in the final image is a multiplication of all the other signals $L_i$, $F$, and $T$ in the frequency domain. Thus, the final image will only have the frequencies that are contained within the three other signals. Figure 14 shows how when we convolve two high-frequency signals, the resulting one keeps the high-frequency content; in contrast, when we convolve a high- and a low-frequency signal, the resulting one has most of its frequencies masked.

We can relate the observations made from Equation (2) to the results on user performance that we obtained from the online behavioral experiments. We have seen that users seem to consistently perform better when they recognize materials from high-frequency geometries and illuminations. This finding is supported by Equation (2) because, to avoid filtering the frequencies of the material in the stimuli, it should have a high-frequency geometry and illumination. Moreover, a low-frequency geometry (or illumination) could filter out the frequencies of the illumination (or geometry) and the material, thus yielding fewer visual features on the final image and, as a result, worse users performance. This finding is consistent with our findings from the analysis of first-order interactions for users performance in Analysis of User Performance and Time.

**Material categories**

We have seen that the reflectance properties seem to be one of the main high-level factors driving material recognition. In this regard, we have also investigated users performance using the classification by reflectance type proposed by *Lagunas et al. (2019)*, where the MERL database is divided into eight different categories with similar reflectance properties. On average, users perform best on *acrylics*, with a top five accuracy of 45.45%, whereas they have their worst performance with *organics*, with an accuracy of 10.22%. Figure 15 shows the top five accuracy for each category in each reference illumination. First, we observe that...
Users performance, in terms of top-5 accuracy, for material recognition tasks taking into account the reflectance of the materials. We can observe how, on average, users perform better for high-frequency illuminations (Uffizi, Grace, and Ennis). Also, we can see how for classes, like fabrics or organics, containing materials with diffuse surface reflectance (low-frequency), users do not have better performance with broad frequency content illuminations. We argue that, since they have a low-frequency surface reflectance, even though there is a high-frequency illumination, those frequencies cannot be represented on the final stimulus that is input to our visual system.

Users seem to perform better with high-frequency illuminations (Uffizi, Grace, Ennis). However, we can see how fabrics and organics do not follow this trend. We argue that fabrics and organics contain mostly materials with a diffuse surface reflectance (low-frequency) that clamp the frequencies of the illumination and, therefore, yield fewer cues in the final stimulus that is input to our visual system.

**Conclusions**

In this work, we have presented a thorough and systematic analysis of the interplay between geometry, illumination, and their spatial frequencies in human performance recognizing materials. We launched rigorous crowd-sourced online behavioral experiments where participants had to solve a material recognition task between a reference and a set of candidate samples. From our experiments, we have observed that, in general, humans seem to be better at recognizing materials in a high-frequency illumination and geometry. We found that simple image statistics, image histograms, and histograms of V1-like subband filters are not capable of capturing human behavior, and, additionally, explored highly nonlinear statistics by training a deep neural network on material classification tasks. We showed that deep neural networks can accurately perform material classification, which suggests that they are capable of encoding and extracting meaningful information from labeled proximal image data. In addition, we gained intuition on which are the main high-level factors that humans and those highly nonlinear statistics use for material recognition and found preliminary evidence that such statistics and humans may share similar high-level factors for material recognition tasks.

**Limitations and future work**

To collect data for the online behavioral experiment we have relied on the Lagunas et al. (2019) dataset which contains images of a diverse set of materials, geometries, and illuminations that faithfully resemble their real-world counterparts. This database focuses on isotropic materials, which are capable of modeling only a subset of real-world materials. A systematic and comprehensive analysis of other heterogeneous materials, or an extension of this study to other nonphotorealistic domains, remains to be done. Our stimuli were rendered using the sphere and Havran geometry, although those surfaces have been widely used in the literature (Havran et al., 2016; Jarabo et al., 2014; Lagunas et al., 2019; Serrano et al., 2016), introducing new geometries could help to further analyze the contribution of the spatial frequencies of the geometry in our perception of material appearance (Nishida & Shinya, 1998).

Moreover, to select our stimuli, we characterized the frequency content of real-world illuminations using the high-frequency content measure (Brossier et al., 2004). We focus on real-world illuminations, which are by definition broadband; therefore, we do not impose or limit their frequency distribution in our analyses; carefully controlling the spatial frequency of the stimuli via filtering to isolate frequency bands and study their individual contribution to the process of material recognition is an interesting avenue of research.

In our additional experiments, we have investigated the asymmetric effect in performance with a high-frequency reference geometry, compared with a high-frequency candidate geometry when all stimuli are displayed at the same size. A rigorous study of the
interplay between display size, the spatial frequencies of the stimuli, and how this affects humans performance on material recognition remains an interesting line of future work. Furthermore, despite the fact that our neural network was trained to classify materials, without any sort of perceptual information, it achieved an agreement with participants answers of 22.43%. This does not prove that the neural network follows the same mechanisms as humans do when performing these tasks. However, this result together with the increase in popularity of deep neural networks, makes the analysis of the perceptual relationship between learned features and the features that our visual system uses to recognize materials a promising avenue to explore. Last, we hope that our analyses will provide relevant insights that will help shed light on the underlying perceptual processes that occur when we recognize materials and, in particular, on how the confounding factors of geometry and illumination affect our perception of material appearance.

Keywords: material recognition, surface geometry, scene illumination, confounding factors, material perception, deep learning

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Footnote

1To simplify the notation we will refer to this geometry as Havran.

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Appendix B: Additional details on the t-STE algorithm

The t-STE algorithm aims to obtain an n-dimensional embedding that satisfies as many qualitative comparisons of the type “A is more similar to B than C” as possible. In our case, a two-dimensional embedding which is easier to visualize. Nevertheless, in the user studies, we have asked participants to select five materials from a pool of candidates and we do not have such qualitative comparisons. However, we can assume that the selection of the users will be closer (more similar) to the reference than any other material that was not selected. Based on this assumption, we generate triplets where the user selection is more similar to the reference material than any other random material that is not within the 5 selected materials. We repeat this process ten times for each of the 5 materials selected by each trial becomes stable as the behavioral experiment advances.

Influence of reference illumination: The reference illumination $I_{ref}$ influences the time users spend to answer each trial ($P = 0.001$). Users spend more time when the stimuli are lit with Ennis illumination while they are the fastest when the illumination is Doge.

We did not find a significant influence of the reference geometry $G_{ref}$ or candidate geometry $G_{cand}$ in the average time each user spent to answer each trial. First order interactions: We observe that users take significantly longer to answer the trials when both the reference geometry and the candidate geometry change ($G_{ref} \times G_{cand}$, $P = 0.001$). This happens in the case where the reference geometry has mostly low spatial frequency content and the candidate geometry changes ($G_{cand} = sphere$, $P = 0.002$); and when the reference has mostly low spatial frequency ($G_{ref} = sphere$, $P = 0.001$) and the candidate geometry changes.

Appendix A: Additional results on the influence of time

Additional details on the time that each participant spent doing the online behavioral experiment. In Figure 16 we can see how the time spent to answer each trial becomes stable as the behavioral experiment advances.

Figure 16. Average time the users spent for each trial according to the order of appearance during the online behavioral experiment. We can observe how, as the user progresses through the experiment, the time spent on each trial becomes stable. The error bars correspond to a 95% confidence interval.
the user making sure that the new randomly sampled material has not been randomly selected already nor that it belongs to the pool of 5 selected materials.

To run the t-STE we set a learning rate of 1, and an \( \alpha = 25 \) (degrees of freedom of the Student-t kernel). Additionally, we apply a logarithmic transformation to the loss value of the t-STE. Those parameters are the same for the answers of the four experiments.

Appendix C: Additional details on image statistics

To measure the correlation between image statistics and users performance we employ a Pearson \( P \) and Spearman \( S \) correlation test with a significance value (\( P \)-value) of 0.05. The value \( P^n \) represents the Pearson correlation for the \( n^{th} \) statistical moment (same applies for the Spearman \( S^n \) correlation).

\[ P = 1 - \frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y}) \]
\[ S = \frac{n \sum_{i=1}^{n} x_i y_i - \sum_{i=1}^{n} x_i \sum_{i=1}^{n} y_i}{\sqrt{[n \sum_{i=1}^{n} x_i^2 - (\sum_{i=1}^{n} x_i)^2][n \sum_{i=1}^{n} y_i^2 - (\sum_{i=1}^{n} y_i)^2]}} \]

**Luminance:** We analyze if the moments of the luminance of each material image have a direct influence on users performance. We found that the moments of the luminance are not correlated with users performance: \( P^1 = -0.14 \) (\( P = 0.17 \)), \( S^1 = -0.15 \) (\( P = 0.15 \)), \( P^2 = 0.02 \) (\( P = 0.83 \)), \( S^2 = -0.03 \) (\( P = 0.78 \)), \( P^3 = 0.03 \) (\( P = 0.77 \)), \( S^3 = 0.03 \) (\( P = 0.78 \)), \( P^4 = 0.01 \) (\( P = 0.94 \)), \( S^4 = 0.05 \) (\( P = 0.65 \)).

**RGB image:** We analyze if the moments of the joint RGB intensity of each material image have a direct influence on users performance. We found that the moments of the joint RGB intensity have little to no correlation with users performance except for the standard deviation: \( P^1 = -0.02 \) (\( P = 0.79 \)), \( S^1 = -0.06 \) (\( P = 0.51 \)), \( P^2 = 0.43 \) (\( P < 0.001 \)), \( S^2 = 0.50 \) (\( P < 0.001 \)), \( P^3 = 0.16 \) (\( P = 0.09 \)), \( S^3 = 0.22 \) (\( P = 0.02 \)), \( P^4 = -0.1 \) (\( P = 0.30 \)), \( S^4 = -0.06 \) (\( P = 0.52 \)).

We also tested out the correlation for each channel and found that for all the channels there is no correlation for any of the first 4 statistical moments.

**Red channel:** On the red channel there seems to be a slight positive linear correlation between the fourth moment (kurtosis) and users performance. All the other statistics show no significant correlation: \( P^1 = -0.10 \) (\( P = 0.29 \)), \( S^1 = -0.08 \) (\( P = 0.42 \)), \( P^2 = 0.03 \) (\( P = 0.60 \)), \( S^2 = -0.02 \) (\( P = 0.87 \)), \( P^3 = 0.07 \) (\( P = 0.46 \)), \( S^3 = 0.07 \) (\( P = 0.51 \)), \( P^4 = 0.20 \) (\( P = 0.04 \)), \( S^4 = 0.15 \) (\( P = 0.13 \)).

**Green channel:** There is no correlation between any statistics on the green channel: \( P^1 = -0.04 \) (\( P = 0.66 \)), \( S^1 = -0.0 \) (\( P = 0.74 \)), \( P^2 = 0.03 \) (\( P = 0.55 \)), \( S^2 = 0.04 \) (\( P = 0.67 \)), \( P^3 = 0.05 \) (\( P = 0.64 \)), \( S^3 = 0.06 \) (\( P = 0.53 \)), \( P^4 = 0.05 \) (\( P = 0.63 \)), \( S^4 = 0.01 \) (\( P = 0.94 \)).

**Blue channel:** Similar to the green channel, the blue does not show any correlation for the first 4 statistical moments: \( P^1 = 0.03 \) (\( P = 0.72 \)), \( S^1 = -0.004 \) (\( P = 0.93 \)), \( P^2 = 0.06 \) (\( P = 0.52 \)), \( S^2 = 0.01 \) (\( P = 0.95 \)), \( P^3 = 0.13 \) (\( P = 0.19 \)), \( S^3 = 0.10 \) (\( P = 0.30 \)), \( P^4 = 0.16 \) (\( P = 0.11 \)), \( S^4 = -0.05 \) (\( P = 0.61 \)).

**Additional results on the SVMs and histogram similarity**

We have trained a total of 6 SVM models, each of them using a different input: RGB pixel intensity, luminance intensity, Gaussian pyramid pixel intensity (Lee & Lee, 2016), Laplacian pyramid pixel intensity (Burt & Adelson, 1983), joining the Gaussian and Laplacian pyramids, and using log-Gabor filters (Fischer et al., 2007). For each of them the SVM achieved a top-5 accuracy in the test set of: 24.17%, 15.16%, 22.50%, 6.33%, 7.52%, and 16.33%, respectively. In addition, we have compared how the SVM predictions agreed with humans’ answers from the online behavioral experiments. For each SVM the agreement is: 4.24%, 4.33%, 4.34%, 5.04%, 4.97%, and 6.36% respectively. Last, we have also computed the histogram similarity using a \( X^2 \) distance. Then, we have taken the five closest samples and compared that with human answers. We do that for each of the five different histograms and each achieves an agreement of: 5.95%, 5.45%, 6.29%, 4.97%, 5.04%, and 5.07% respectively.

Appendix D: Additional details on ResNet training

To train the 35 layers ResNet (34 of the original model plus an additional fully connected) (He et al., 2016) we have employed the dataset introduced by Lagunas et al. (Lagunas et al., 2019), which contains renderings of materials with different illuminations and geometries. We keep the images rendered with Havran-3 geometry for validation purposes and Havran geometry for testing. All the other images are used for training. To train the model to classify materials we use a soft cross-entropy loss where samples that do not belong to the same class are penalized (Szegedy et al., 2015). The loss function takes the probabilities output of the softmax layer and penalizes when they give a high probability to the materials that do not belong to the input image. The images input to the model are resized to 224 × 224 pixels. The parameters of the model are initialized using a pretrained version on ImageNet dataset (Deng et al., 2009). We use the ADAM algorithm (Kingma & Ba, 2014) as the optimizer. The model has been trained during 50 iterations starting at a learning rate of \( 10^{-3} \) and decayed by a factor of 10 at the iteration 20, 35, and 45; the batch-size was set to 64 images. We use the PyTorch framework and use an Nvidia 2080Ti GPU.